



# Algebraic Expressions and Identities

## Understanding the Lesson

- Algebraic expression and its elements.
- Terms, Factors and Coefficients.
- Monomials, Binomials and Polynomials.
- Like and unlike terms.
- Addition and Subtraction of Algebraic function.
- Multiplication of Algebraic Expressions.
- Multiplication of monomial by a monomial.
- Multiplication of a monomial by a polynomial.
- Multiplication of a polynomial by a polynomial.
- Multiplication of a binomial by a trinomial.
- Standard Identities.

## Conceptual Facts

- **Algebraic Expression:** A combination of numbers which includes literal number connected by the symbols +, −, × and ÷ is called an algebraic expression.

For example:  $5x$ ,  $8x - 3$ ,  $2x + 3y$ ,  $\frac{3}{4}x^2$ ,  $4xyz$  are some algebraic expressions.

Here, 5, 8, 3, 2,  $\frac{3}{4}$  and 4 are constants and the literal numbers are  $x$ ,  $y$  and  $z$ .

The different parts of the expression are called terms.

$5x$ ,  $8x$ ,  $2x$ ,  $3y$ ,  $\frac{3x^2}{4}$  etc., are all the terms.

**Coefficient:** A coefficient is a multiplicative factor in some term of a polynomial. It is usually a number, but may be only expression along.

For example in  $7x^2 - 3xy + y + 3$ . The first three terms respectively have coefficient 7, −3 and 3 is a constant in given polynomial.

- **Monomial:** The expression having only one term is called monomial.  
For example:  $3x$ ,  $8xy$ ,  $6x^2$ ,  $11xyz$ , etc.
- **Binomial:** The expression containing two terms is called binomial.  
For example:  $2x + y$ ,  $x + y$ ,  $3xy - 5z$ ,  $\frac{1}{2}xy + 5$ , etc.
- **Trinomial:** The expression containing three terms is called trinomial.  
For example:  $x + 2y + 3$ ,  $xy - z + \frac{1}{2}$ ,  $\frac{1}{2}x^2 + 2x + 5$ , etc.
- **Polynomial:** Algebraic expression containing one or more terms with non-zero coefficient is called a polynomial.  
For example:  $2 + 3x$ ,  $x + y + 3z - 5$ ,  $\frac{1}{2}x^2 + yz - 5$ , etc.
- **Like and Unlike Terms:** Algebraic expressions having same combination of literal numbers are called like terms.

For example:  $4xy$ ,  $-5xy$ ,  $\frac{17}{3}xy$ , are like terms.

Algebraic expressions having different combinations of literal numbers are called unlike terms.

For example:  $(xy, yz, zx)$ ,  $(2x^2, -5xy^2, 7xyz)$ ,  $(3, -5x, 7yz)$  etc.

- **Degree of Algebraic Expression:** Highest power of the variable of an algebraic expression is called its degree.

For example: Degree of  $3x^2 - 7x + 5$  is 2.

- **Addition or Subtraction of two or more polynomials:**

(i) Collect the like terms together.

(ii) Find the sum or difference of the numerical coefficients of these terms.

**For example:**

(i) Add:  $2x^2y^3, -5x^2y^3 + \frac{11}{2}x^2y^3$

Sol.  $2x^2y^3 + (-5x^2y^3) + \left(\frac{11}{2}x^2y^3\right) = \left(2 - 5 + \frac{11}{2}\right)x^2y^3 = \frac{5}{2}x^2y^3$

(ii) Subtract:  $(3x - 5)$  from  $(8x - 25)$

Sol. 
$$\begin{array}{r} 8x - 25 \\ 3x - 5 \\ \hline (-) (+) \\ \hline 5x - 20 \end{array}$$
 [Arrange the terms columnwise and change the sign of and add]

**Multiplication Rule of Signs:**

$$\begin{aligned} (+x) \times (+y) &= (+xy) \\ (+x) \times (-y) &= (-xy) \\ (-x) \times (y) &= (-xy) \\ (-x) \times (-y) &= (+xy) \end{aligned}$$

**TRY THESE (PAGE 138)**

**Q1.** Give five examples of expressions containing one variable and five examples of expressions containing two variables.

**Sol.** Expressions containing one variable:

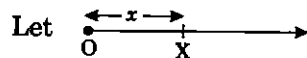
$$3x, \frac{1}{2}y, 5z, 3x^2, \frac{1}{2}z$$

Expressions containing two variables:

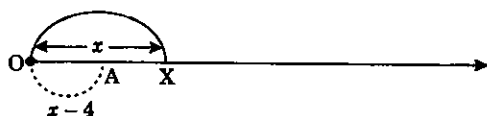
$$x + y, xy + 4, 3x - \frac{1}{2}y, xz, 5x^2 + 3y$$

**Q2.** Show on the number line  $x, x - 4, 2x + 1, 3x - 2$

**Sol.**  $x$



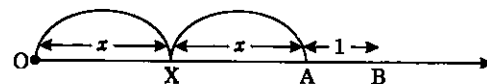
$x - 4$



Here,  $OX = x$  and  $XA = -4$

$\therefore OA = x - 4$

$\Rightarrow 2x + 1$

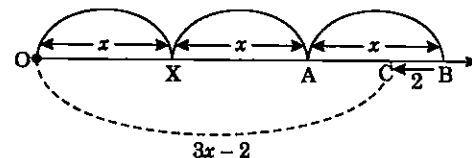


Here,  $OX = x, XA = x$

$\Rightarrow OA = 2x$

and  $AB = 1$  unit

$\Rightarrow 3x - 2$



Here,  $OX = XA = AB = x$

$\Rightarrow OB = 3x$

$BC = 2$  unit

$\Rightarrow OC = 3x - 2$

**TRY THESE (PAGE 138)**

**Q1.** Classify the following polynomials as monomials, binomials, trinomials.

$-z + 5, x + y + z, y + z + 100, ab - ac, 17$

**Sol.** Monomials: 17

Binomials:  $-z + 5, ab - ac$

Trinomials:  $x + y + z, y + z + 100$

**Q2.** Construct:

(a) 3 binomials with only  $x$  as a variable.

(b) 3 binomials with  $x$  and  $y$  as variables.

(c) 3 monomials with  $x$  and  $y$  as variables.

(d) 2 polynomials with 4 or more terms.

**Sol.** (a)  $x + 2, 3x - 1$  and  $\frac{1}{2}x + 3$

(b)  $x + y, 2x - 3y$  and  $\frac{1}{2}x - \frac{3}{4}y$

(c)  $xy, 2xy, -3yx$

(d)  $x + y + z - 1$  and  $2x + 3y - z + w - 5$

**TRY THESE (PAGE 139)**

**Q1.** Write two terms which are like

(i)  $7xy$  (ii)  $4mn^2$  (iii)  $2l$

**Sol.** (i)  $7xy, 5xy, -3xy$  and  $\frac{2}{5}xy$  are all like terms.

(ii)  $4mn^2, -2mn^2, 6mn^2$  and  $\frac{1}{2}mn^2$  are all like terms.

(iii)  $2l, 3l, 4l$  and  $\frac{1}{2}l$  are all like terms.

**EXERCISE 9.1**

**Q1.** Identify the terms, their coefficients for each of the following expressions.

(i)  $5xyz^2 - 3zy$

(ii)  $1 + x + x^2$

(iii)  $4x^2y^2 - 4x^2y^2z^2 + z^2$

(iv)  $3 - pq + qr - rp$

(v)  $\frac{x}{2} + \frac{y}{2} - xy$

(vi)  $0.3a - 0.6ab + 0.5b$

Expression	Terms	Coefficients
(i) $5xyz^2 - 3zy$	$5xyz^2$	5
	$-3zy$	-3
(ii) $1 + x + x^2$	1	1
	$x$	1
	$x^2$	1
(iii) $4x^2y^2 - 4x^2y^2z^2 + z^2$	$4x^2y^2$	4
	$-4x^2y^2z^2$	-4
	$z^2$	1

(iv) $3 - pq + qr - rp$	3	3
	$-pq$	-1
	$qr$	1
	$-rp$	-1
(v) $\frac{x}{2} + \frac{y}{2} - xy$	$\frac{x}{2}$	$\frac{1}{2}$
	$\frac{y}{2}$	$\frac{1}{2}$
	$-xy$	-1
(vi) $0.3a - 0.6ab + 0.5b$	$0.3a$	0.3
	$-0.6ab$	-0.6
	$0.5b$	0.5

Expression	Category
(i) $x + y$	binomial
(ii) 1000	monomial
(iii) $x + x^2 + x^3 + x^4$	polynomial → does not fit in the given categories
(iv) $7 + y + 5x$	trinomial
(v) $2y - 3y^2$	binomial
(vi) $2y - 3y^2 + 4y^3$	trinomial
(vii) $5x - 4y + 3xy$	trinomial
(viii) $4z - 15z^2$	binomial
(ix) $ab + bc + cd + da$	polynomial → does not fit in the given categories
(x) $pqr$	monomial
(xi) $p^2q + pq^2$	binomial
(xii) $2p + 2q$	binomial

**Q2.** Classify the following polynomials as monomials, binomials, trinomials. Which polynomials do not fit in any of these three categories?

$x + y, 1000, x + x^2 + x^3 + x^4, 7 + y + 5x, 2y - 3y^2, 2y - 3y^2 + 4y^3, 5x - 4y + 3xy, 4z - 15z^2, ab + bc + cd + da, pqr, p^2q + pq^2, 2p + 2q$

**Q3.** Add the following:

(i)  $ab - bc, bc - ca, ca - ab$

(ii)  $a - b + ab, b - c + bc, c - a + ac$

(iii)  $2p^2q^2 - 3pq + 4, 5 + 7pq - 3p^2q^2$

(iv)  $l^2 + m^2, m^2 + n^2, n^2 + l^2, 2lm + 2mn + 2nl$

**Sol.** (i) **Given:**  $ab - bc, bc - ca, ca - ab$

We have

$$(ab - bc) + (bc - ca) + (ca - ab)$$

(Adding all the terms)

$$= ab - bc + bc - ca + ca - ab$$

$$= (ab - ab) + (bc - bc) + (ca - ca)$$

(Collecting the like terms together)

$$= 0 + 0 + 0 = 0$$

(ii) **Given:**

$$a - b + ab, b - c + bc, c - a + ac$$

We have  $(a - b + ab) + (b - c + bc)$

$$+ (c - a + ac)$$

(Adding all the terms)

$$= a - b + ab + b - c + bc + c - a + ac$$

$$= (a - a) + (b - b) + (c - c) + ab + bc + ac$$

(Collecting all the like terms together)

$$= 0 + 0 + 0 + ab + bc + ac$$

$$= ab + bc + ac$$

(iii) **Given:**

$$2p^2q^2 - 3pq + 4, 5 + 7pq - 3p^2q^2$$

By arranging the like terms in the same column, we have

$$2p^2q^2 - 3pq + 4$$

$$-3p^2q^2 + 7pq + 5$$

+

$$- p^2q^2 + 4pq + 9$$

(Adding columnwise)

(iv) **Given:**  $l^2 + m^2, m^2 + n^2, n^2 + l^2, 2lm + 2mn + 2nl$

By arranging the like terms in the same column, we have

$$l^2 + m^2$$

$$+ m^2 + n^2$$

$$l^2 + n^2$$

+

$$2lm + 2mn + 2nl$$

$$2l^2 + 2m^2 + 2n^2 + 2lm + 2mn + 2nl$$

(Adding columnwise)

Thus, the sum of the given expressions is  $2(l^2 + m^2 + n^2 + lm + mn + nl)$

**Q4.** (a) Subtract  $4a - 7ab + 3b + 12$  from  $12a - 9ab + 5b - 3$

(b) Subtract  $3xy + 5yz - 7zx$  from  $5xy - 2yz - 2zx + 10xyz$

(c) Subtract  $4p^2q - 3pq + 5pq^2 - 8p + 7q - 10$  from  $18 - 3p - 11q + 5pq - 2pq^2 + 5p^2q$

**Sol.** (a) Arranging the like terms columnwise, we have

$$12a - 9ab + 5b - 3$$

$$4a - 7ab + 3b + 12$$

$$\begin{array}{r} (-) \quad (+) \quad (-) \quad (-) \\ \hline \end{array}$$

$$8a - 2ab + 2b - 15$$

[Change the signs of all the terms of lower expressions and then add]

(b) Arranging the like terms columnwise, we have

$$5xy - 2yz - 2zx + 10xyz$$

$$3xy + 5yz - 7zx + 0$$

$$\begin{array}{r} (-) \quad (-) \quad (+) \quad (-) \\ \hline \end{array}$$

$$2xy - 7yz + 5zx + 10xyz$$

[Change the signs of all the terms of lower expressions and then add]

(c) Arranging the like terms columnwise, we have

$$18 - 3p - 11q + 5pq - 2pq^2 + 5p^2q$$

$$-10 - 8p + 7q - 3pq + 5p^2q + 4p^2q$$

$$\begin{array}{r} (+) \quad (+) \quad (-) \quad (+) \quad (-) \quad (-) \\ \hline \end{array}$$

$$20 + 5p - 18q + 8pq - 7pq^2 + p^2q$$

[Change the signs of all the terms of lower expressions and then add]

The terms are  $p^2q - 7pq^2 + 8pq - 18q + 5p + 20$

**TRY THESE (PAGE 142)**

Can you think of two more such situations, where we may need to multiply algebraic expressions?

- Hint:**
- Think of speed and time;
  - Think of interest to be paid, the principal and the rate of simple interest, etc.

Sol. Yes,

**Situation I:** We think about the area of a rectangle whose length is  $x$  and breadth is  $y$ .

$$\begin{aligned} \therefore \text{Area of the rectangle} &= \text{length} \times \text{breadth} \\ &= xy \text{ sq units} \end{aligned}$$

If the length is increased by 5 units and the breadth is decreased by 2 units, then the area of the rectangle

$$= (x + 5) \times (y - 2) \text{ sq units}$$

**Situation II:** Let a body take  $t$  hours to cover a certain distance at the rate of  $u$  km/h

$$\begin{aligned} \therefore \text{Distance covered} &= \text{speed} \times \text{time} \\ &= u \times t \text{ km} \end{aligned}$$

If the speed is increased by 3 km/h and the time is decreased by 5 hours, then the distance covered

$$= (u + 3) \times (t - 5) \text{ km}$$

**TRY THESE (PAGE 143)**

**Q1.** Find  $4x \times 5y \times 7z$

First find  $4x \times 5y$  and multiply it by  $7z$ ; or first find  $5y \times 7z$  and multiply it by  $4x$ .

Is the result the same? What do you observe?

Does the order in which you carry out the multiplication matter?

**Sol. Method I:**  $(4x \times 5y) \times 7z$

$$20xy \times 7z = 140xyz$$

**Method II:**  $(5y \times 7z) \times 4x$

$$= 35yz \times 4x$$

$$= 140xyz \text{ same result}$$

Thus we observe that the order of the terms in multiplication does not matter.

**EXERCISE 9.2**

**Q1.** Find the product of the following pairs of monomials.

- (i)  $4, 7p$       (ii)  $-4p, 7p$   
 (iii)  $-4p, 7pq$       (iv)  $4p^3, -3p$       (v)  $4p, 0$

**Sol.** (i)  $4 \times 7p = (4 \times 7) \times p = 28p$   
 (ii)  $-4p \times 7p = (-4 \times 7) \times p \times p = -28p^2$   
 (iii)  $-4p \times 7pq = (-4 \times 7) \times p \times pq = -28p^2q$   
 (iv)  $4p^3 \times -3p = (4 \times -3) \times p^3 \times p = -12p^4$   
 (v)  $4p \times 0 = (4 \times 0) \times p = 0 \times p = 0$

**Q2.** Find the areas of rectangles with the following pairs of monomials as their lengths and breadths respectively.

- $(p, q); (10m, 5n); (20x^2, 5y^2); (4x, 3x^2); (3mn, 4np)$

**Sol.** (i) Length =  $p$  units and breadth =  $q$  units  
 Area of the rectangle  
 = length  $\times$  breadth  
 =  $p \times q = pq$  sq units  
 (ii) Length =  $10m$  units, breadth =  $5n$  units  
 $\therefore$  Area of the rectangle  
 = length  $\times$  breadth  
 =  $10m \times 5n$

=  $(10 \times 5) \times m \times n$   
 =  $50mn$  sq units  
 (iii) Length =  $20x^2$  units, breadth =  $5y^2$  units  
 $\therefore$  Area of the rectangle  
 = length  $\times$  breadth  
 =  $20x^2 \times 5y^2$   
 =  $(20 \times 5)x^2 \times y^2$   
 =  $100x^2y^2$  sq units  
 (iv) Length =  $4x$  units, breadth =  $3x^2$  units  
 $\therefore$  Area of the rectangle  
 = length  $\times$  breadth  
 =  $4x \times 3x^2$   
 =  $(4 \times 3) \times x \times x^2$   
 =  $12x^3$  sq units  
 (v) Length =  $3mn$  units, breadth =  $4np$  units  
 $\therefore$  Area of the rectangle  
 = length  $\times$  breadth  
 =  $3mn \times 4np$   
 =  $(3 \times 4) \times mn \times np$   
 =  $12mn^2p$  sq units

**Q3.** Complete the table of products.

First monomial $\rightarrow$	$2x$	$-5y$	$3x^2$	$-4xy$	$7x^2y$	$-9x^2y^2$
Second monomial $\downarrow$						
$2x$	$4x^2$	-	-	-	-	-
$-5y$	-	-	$-15x^2y$	-	-	-
$3x^2$	-	-	-	-	-	-
$-4xy$	-	-	-	-	-	-
$7x^2y$	-	-	-	-	-	-
$-9x^2y^2$	-	-	-	-	-	-

Sol. Completed table

First monomial →	2x	-5y	3x <sup>2</sup>	-4xy	7x <sup>2</sup> y	-9x <sup>2</sup> y <sup>2</sup>
Second monomial ↓						
2x	4x <sup>2</sup>	-10xy	6x <sup>3</sup>	-8x <sup>2</sup> y	14x <sup>3</sup> y	-18x <sup>3</sup> y <sup>2</sup>
-5y	-10xy	25y <sup>2</sup>	-15x <sup>2</sup> y	20x <sup>2</sup> y	-35x <sup>2</sup> y <sup>2</sup>	45x <sup>2</sup> y <sup>3</sup>
3x <sup>2</sup>	6x <sup>3</sup>	-15x <sup>2</sup> y	9x <sup>4</sup>	-12x <sup>3</sup> y	21x <sup>4</sup> y	-27x <sup>4</sup> y <sup>2</sup>
-4xy	-8x <sup>2</sup> y	20xy <sup>2</sup>	-12x <sup>3</sup> y	16x <sup>2</sup> y <sup>2</sup>	-28x <sup>3</sup> y <sup>2</sup>	36x <sup>3</sup> y <sup>3</sup>
7x <sup>2</sup> y	14x <sup>3</sup> y	-35x <sup>2</sup> y <sup>2</sup>	21x <sup>4</sup> y	-28x <sup>3</sup> y <sup>2</sup>	49x <sup>4</sup> y <sup>2</sup>	-63x <sup>4</sup> y <sup>3</sup>
-9x <sup>2</sup> y <sup>2</sup>	-18x <sup>3</sup> y <sup>2</sup>	45x <sup>2</sup> y <sup>3</sup>	-27x <sup>4</sup> y <sup>2</sup>	36x <sup>3</sup> y <sup>3</sup>	-63x <sup>4</sup> y <sup>3</sup>	81x <sup>4</sup> y <sup>4</sup>

Q4. Obtain the volume of rectangular boxes with the following length, breadth and height respectively.

(i)  $5a, 3a^2, 7a^4$

(ii)  $2p, 4q, 8r$

(iii)  $xy, 2x^2y, 2xy^2$

(iv)  $a, 2b, 3c$

Sol. (i) Here, length =  $5a$ , breadth =  $3a^2$ , height =  $7a^4$

Volume of the box

$$= l \times b \times h$$

$$= 5a \times 3a^2 \times 7a^4$$

$$= 105 a^7 \text{ cu. units}$$

(ii) Here, length =  $2p$ , breadth =  $4q$ , height =  $8r$

Volume of the box

$$= l \times b \times h$$

$$= 2p \times 4q \times 8r$$

$$= 64pqr \text{ cu. units}$$

(iii) Here, length =  $xy$ , breadth =  $2x^2y$ , height =  $2xy^2$

Volume of the box

$$= l \times b \times h$$

$$= xy \times 2x^2y \times 2xy^2$$

$$= (1 \times 2 \times 2) \times xy \times x^2y \times xy^2$$

$$= 4x^4y^4 \text{ cu. units}$$

(iv) Here, length =  $a$ , breadth =  $2b$ , height =  $3c$

Volume of the box

$$= \text{length} \times \text{breadth} \times \text{height}$$

$$= a \times 2b \times 3c$$

$$= (1 \times 2 \times 3)abc$$

$$= 6 abc \text{ cu. units}$$

Q5. Obtain the product of

(i)  $xy, yz, zx$

(ii)  $a, -a^2, a^3$

(iii)  $2, 4y, 8y^2, 16y^3$

(iv)  $a, 2b, 3c, 6abc$

(v)  $m, -mn, mnp$

Sol. (i)  $xy \times yz \times zx = x^2y^2z^2$

(ii)  $a \times (-a^2) \times a^3 = -a^6$

(iii)  $2 \times 4y \times 8y^2 \times 16y^3$

$$= (2 \times 4 \times 8 \times 16) \times y \times y^2 \times y^3$$

$$= 1024y^6$$

(iv)  $a \times 2b \times 3c \times 6abc$

$$= (1 \times 2 \times 3 \times 6) \times a \times b \times c \times abc$$

$$= 36a^2b^2c^2$$

(v)  $m \times (-mn) \times mnp$

$$= [1 \times (-1) \times 1]m \times mn \times mnp$$

$$= -m^3n^2p$$

TRY THESE (PAGE 144)

Q1. Find the product:

(i)  $2x(3x + 5xy)$

(ii)  $a^2(2ab - 5c)$

Sol. (i)  $2x(3x + 5xy)$

$$= (2x \times 3x) + (2x \times 5xy) = 6x^2 + 10x^2y$$

(ii)  $a^2(2ab - 5c)$

$$= (a^2 \times 2ab) - (a^2 \times 5c) = 2a^3b - 5a^2c$$

TRY THESE (PAGE 145)

Q1. Find the product:  $(4p^2 + 5p + 7) \times 3p$

Sol.  $(4p^2 + 5p + 7) \times 3p$

$$= (4p^2 \times 3p) + (5p \times 3p) + (7 \times 3p)$$

$$= 12p^3 + 15p^2 + 21p$$

### EXERCISE 9.3

Q1. Carry out the multiplication of the expressions in each of the following pairs:

(i)  $4p, q + r$

(ii)  $ab, a - b$

(iii)  $a + b, 7a^2b^2$

(iv)  $a^2 - 9, 4a$

(v)  $pq + qr + rp, 0$

Sol. (i)  $4p \times (q + r) = (4p \times q) + (4p \times r)$

$$= 4pq + 4pr$$

(ii)  $ab, a - b = ab \times (a - b)$

$$= (ab \times a) - (ab \times b)$$

$$= a^2b - ab^2$$

$$(iii) (a + b) \times 7a^2b^2$$

$$= (a \times 7a^2b^2) + (b \times 7a^2b^2)$$

$$= 7a^3b^2 + 7a^2b^3$$

$$(iv) (a^2 - 9) \times 4a = (a^2 \times 4a) - (9 \times 4a)$$

$$= 4a^3 - 36a$$

$$(v) (pq + qr + rp) \times 0 = 0$$

[∵ Any number multiplied by 0 is = 0]

**Q2.** Complete the table.

S. No.	First expression	Second expression	Product
(i)	$a$	$b + c + d$	-
(ii)	$x + y - 5$	$5xy$	-
(iii)	$p$	$6p^2 - 7p + 5$	-
(iv)	$4p^2q^2$	$p^2 - q^2$	-
(v)	$a + b + c$	$abc$	-

**Sol.**

(i)  $a \times (b + c + d)$   
 $= (a \times b) + (a \times c) + (a \times d)$   
 $= ab + ac + ad$

(ii)  $(x + y - 5) (5xy)$   
 $= (x \times 5xy) + (y \times 5xy) - (5 \times 5xy)$   
 $= 5x^2y + 5xy^2 - 25xy$

(iii)  $p \times (6p^2 - 7p + 5)$   
 $= (p \times 6p^2) - (p \times 7p) + (p \times 5)$   
 $= 6p^3 - 7p^2 + 5p$

(iv)  $4p^2q^2 \times (p^2 - q^2)$   
 $= 4p^2q^2 \times p^2 - 4p^2q^2 \times q^2$   
 $= 4p^4q^2 - 4p^2q^4$

(v)  $(a + b + c) \times (abc)$   
 $= (a \times abc) + (b \times abc) + (c \times abc)$   
 $= a^2bc + ab^2c + abc^2$

**Completed Table:**

S. No.	First expression	Second expression	Product
(i)	$a$	$b + c + d$	$ab + ac + ad$
(ii)	$x + y - 5$	$5xy$	$5x^2y + 5xy^2 - 25xy$
(iii)	$p$	$6p^2 - 7p + 5$	$6p^3 - 7p^2 + 5p$
(iv)	$4p^2q^2$	$p^2 - q^2$	$4p^4q^2 - 4p^2q^4$
(v)	$a + b + c$	$abc$	$a^2bc + ab^2c + abc^2$

**Q3.** Find the products.

(i)  $(a^2) \times (2a^{22}) \times (4a^{26})$

(ii)  $\left(\frac{2}{3}xy\right) \times \left(-\frac{9}{10}x^2y^2\right)$

(iii)  $\left(-\frac{10}{3}pq^3\right) \times \left(\frac{6}{5}p^3q\right)$

(iv)  $x \times x^2 \times x^3 \times x^4$

**Sol.**

(i)  $(a^2) \times (2a^{22}) \times (4a^{26})$   
 $= 1 \times 2 \times 4 \times a^{2+22+26}$   
 $= 8a^{50}$

(ii)  $\left(\frac{2}{3}xy\right) \times \left(-\frac{9}{10}x^2y^2\right)$   
 $= \frac{2}{3} \times \left(-\frac{9}{10}\right) \times x^{1+2} \cdot y^{1+2}$   
 $= -\frac{3}{5} \cdot x^3y^3$

(iii)  $\left(-\frac{10}{3}pq^3\right) \times \left(\frac{6}{5}p^3q\right)$   
 $= \left(-\frac{10}{3}\right) \times \left(\frac{6}{5}\right) \times p^{1+3}q^{3+1}$   
 $= -4p^4q^4$

(iv)  $x \times x^2 \times x^3 \times x^4$   
 $= x^{1+2+3+4} = x^{10}$

**Q4.** (a) Simplify:  $3x(4x - 5) + 3$  and find its values

for (i)  $x = 3$  (ii)  $x = \frac{1}{2}$ .

(b) Simplify:  $a(a^2 + a + 1) + 5$  and find its value for (i)  $a = 0$  (ii)  $a = 1$  (iii)  $a = -1$

**Sol.** (a) We have  $3x(4x - 5) + 3$   
 $= 4x \times 3x - 5 \times 3x + 3$   
 $= 12x^2 - 15x + 3$

(i) For  $x = 3$ , we have  
 $12 \times (3)^2 - 15 \times 3 + 3$   
 $= 12 \times 9 - 45 + 3$   
 $= 108 - 42 = 66$

(ii) For  $x = \frac{1}{2}$ , we have

$$12\left(\frac{1}{2}\right)^2 - 15\left(\frac{1}{2}\right) + 3$$

$$= 12 \times \frac{1}{4} - \frac{15}{2} + 3$$

$$= 3 - \frac{15}{2} + 3$$

$$= \frac{6 - 15 + 6}{2} = \frac{12 - 15}{2} = -\frac{3}{2}$$

(b) We have  $a(a^2 + a + 1) + 5$   
 $= (a^2 \times a) + (a \times a) + (1 \times a) + 5$   
 $= a^3 + a^2 + a + 5$

(i) For  $a = 0$ , we have  
 $= (0)^3 + (0)^2 + (0) + 5 = 5$

(ii) For  $a = 1$ , we have  
 $= (1)^3 + (1)^2 + (1) + 5$   
 $= 1 + 1 + 1 + 5 = 8$

$$\begin{aligned} \text{(iii) For } a = -1, \text{ we have} \\ &= (-1)^3 + (-1)^2 + (-1) + 5 \\ &= -1 + 1 - 1 + 5 = 4 \end{aligned}$$

- Q5.** (a) Add:  $p(p - q)$ ,  $q(q - r)$  and  $r(r - p)$   
 (b) Add:  $2x(z - x - y)$  and  $2y(z - y - x)$   
 (c) Subtract:  $3l(l - 4m + 5n)$  from  $4l(10n - 3m + 2l)$   
 (d) Subtract:  $3a(a + b + c) - 2b(a - b + c)$  from  $4c(-a + b + c)$

**Sol.** (a)  $p(p - q) + q(q - r) + r(r - p)$   
 $= (p \times p) - (p \times q) + (q \times q) - (q \times r)$   
 $\quad\quad\quad + (r \times r) - (r \times p)$   
 $= p^2 - pq + q^2 - qr + r^2 - rp$   
 $= p^2 + q^2 + r^2 - pq - qr - rp$

(b)  $2x(z - x - y) + 2y(z - y - x)$   
 $= (2x \times z) - (2x \times x) - (2x \times y) +$   
 $\quad\quad\quad (2y \times z) - (2y \times y) - (2y \times x)$   
 $= 2xz - 2x^2 - 2xy + 2yz - 2y^2 - 2xy$

$$\begin{aligned} &= -2x^2 - 2y^2 + 2xz + 2yz - 4xy \\ &= -2x^2 - 2y^2 - 4xy + 2yz + 2xz \\ \text{(c) } &4l(10n - 3m + 2l) - 3l(l - 4m + 5n) \\ &= (4l \times 10n) - (4l \times 3m) + (4l \times 2l) \\ &\quad - (3l \times l) - (3l \times -4m) - (3l \times 5n) \\ &= 40ln - 12lm + 8l^2 - 3l^2 + 12lm - 15ln \\ &= (40ln - 15ln) + (-12lm + 12lm) \\ &\quad\quad\quad + (8l^2 - 3l^2) \\ &= 25ln + 0 + 5l^2 \\ &= 25ln + 5l^2 \Rightarrow 5l^2 + 25ln \\ \text{(d) } &[4c(-a + b + c)] - [3a(a + b + c) \\ &\quad\quad\quad - 2b(a - b + c)] \\ &= (-4ac + 4bc + 4c^2) - (3a^2 + 3ab \\ &\quad\quad\quad + 3ac - 2ab + 2b^2 - 2bc) \\ &= -4ac + 4bc + 4c^2 - 3a^2 - 3ab - 3ac \\ &\quad\quad\quad + 2ab - 2b^2 + 2bc \\ &= -3a^2 - 2b^2 + 4c^2 - ab + 6bc - 7ac \end{aligned}$$

### EXERCISE 9.4

**Q1.** Multiply the binomials:

- (i)  $(2x + 5)$  and  $(4x - 3)$   
 (ii)  $(y - 8)$  and  $(3y - 4)$   
 (iii)  $(2.5l - 0.5m)$  and  $(2.5l + 0.5m)$   
 (iv)  $(a + 3b)$  and  $(x + 5)$   
 (v)  $(2pq + 3q^2)$  and  $(3pq - 2q^2)$   
 (vi)  $\left(\frac{3}{4}a^2 + 3b^2\right)$  and  $4\left(a^2 - \frac{2}{3}b^2\right)$

**Sol.** (i)  $(2x + 5) \times (4x - 3)$   
 $= 2x \times (4x - 3) + 5 \times (4x - 3)$   
 $= (2x \times 4x) - (3 \times 2x) + (5 \times 4x) - (5 \times 3)$   
 $= 8x^2 - 6x + 20x - 15$   
 $= 8x^2 + 14x - 15$

(ii)  $(y - 8) \times (3y - 4)$   
 $= y \times (3y - 4) - 8 \times (3y - 4)$   
 $= (y \times 3y) - (y \times 4) - (8 \times 3y) + (-8 \times -4)$   
 $= 3y^2 - 4y - 24y + 32$   
 $= 3y^2 - 28y + 32$

(iii)  $(2.5l - 0.5m) \times (2.5l + 0.5m)$   
 $= (2.5l \times 2.5l) + (2.5l \times 0.5m)$   
 $\quad - (0.5m \times 2.5l) - (0.5m \times 0.5m)$   
 $= 6.25l^2 + 1.25ml - 1.25ml - 0.25m^2$   
 $= 6.25l^2 + 0 - 0.25m^2$   
 $= 6.25l^2 - 0.25m^2$

(iv)  $(a + 3b) \times (x + 5)$   
 $= a \times (x + 5) + 3b \times (x + 5)$   
 $= (a \times x) + (a \times 5) + (3b \times x) + (3b \times 5)$   
 $= ax + 5a + 3bx + 15b$

(v)  $(2pq + 3q^2) \times (3pq - 2q^2)$   
 $= 2pq \times (3pq - 2q^2) + 3q^2 (3pq - 2q^2)$   
 $= (2pq \times 3pq) - (2pq \times 2q^2)$   
 $\quad + (3q^2 \times 3pq) - (3q^2 \times 2q^2)$   
 $= 6p^2q^2 - 4pq^3 + 9pq^3 - 6q^4$   
 $= 6p^2q^2 + 5pq^3 - 6q^4$

(vi)  $\left(\frac{3}{4}a^2 + 3b^2\right) \times 4\left(a^2 - \frac{2}{3}b^2\right)$   
 $= \left(\frac{3}{4}a^2 + 3b^2\right) \times \left(4a^2 - \frac{8}{3}b^2\right)$   
 $= \frac{3}{4}a^2 \times \left(4a^2 - \frac{8}{3}b^2\right)$   
 $\quad + 3b^2 \times \left(4a^2 - \frac{8}{3}b^2\right)$   
 $= \left(\frac{3}{4}a^2 \times 4a^2\right) - \left(\frac{3}{4}a^2 \times \frac{8}{3}b^2\right)$   
 $\quad + (3b^2 \times 4a^2) - \left(3b^2 \times \frac{8}{3}b^2\right)$   
 $= 3a^4 - 2a^2b^2 + 12a^2b^2 - 8b^4$   
 $= 3a^4 + 10a^2b^2 - 8b^4$

**Q2.** Find the product:

- (i)  $(5 - 2x)(3 + x)$       (ii)  $(x + 7y)(7x - y)$   
 (iii)  $(a^2 + b)(a + b^2)$       (iv)  $(p^2 - q^2)(2p + q)$

**Sol.** (i)  $(5 - 2x)(3 + x)$   
 $= 5(3 + x) - 2x(3 + x)$   
 $= (5 \times 3) + (5 \times x) - (2x \times 3) - (2x \times x)$   
 $= 15 + 5x - 6x - 2x^2$   
 $= 15 - x - 2x^2$



$$\begin{aligned} \text{(ii)} \quad & (x + 7y)(7x - y) \\ &= x(7x - y) + 7y(7x - y) \\ &= (x \times 7x) - (x \times y) + (7y \times 7x) - (7y \times y) \\ &= 7x^2 - xy + 49xy - 7y^2 \\ &= 7x^2 + 48xy - 7y^2 \end{aligned}$$

$$\begin{aligned} \text{(iii)} \quad & (a^2 + b)(a + b^2) \\ &= a^2(a + b^2) + b(a + b^2) \\ &= (a^2 \times a) + (a^2 \times b^2) + (b \times a) + (b \times b^2) \\ &= a^3 + a^2b^2 + ab + b^3 \end{aligned}$$

$$\begin{aligned} \text{(iv)} \quad & (p^2 - q^2)(2p + q) \\ &= p^2(2p + q) - q^2(2p + q) \\ &= (p^2 \times 2p) + (p^2 \times q) - (q^2 \times 2p) - (q^2 \times q) \\ &= 2p^3 + p^2q - 2pq^2 - q^3 \end{aligned}$$

**Q3. Simplify:**

$$\text{(i)} \quad (x^2 - 5)(x + 5) + 25$$

$$\text{(ii)} \quad (a^2 + 5)(b^3 + 3) + 5$$

$$\text{(iii)} \quad (t + s^2)(t^2 - s)$$

$$\text{(iv)} \quad (a + b)(c - d) + (a - b)(c + d) + 2(ac + bd)$$

$$\text{(v)} \quad (x + y)(2x + y) + (x + 2y)(x - y)$$

$$\text{(vi)} \quad (x + y)(x^2 - xy + y^2)$$

$$\text{(vii)} \quad (1.5x - 4y)(1.5x + 4y + 3) - 4.5x + 12y$$

$$\text{(viii)} \quad (a + b + c)(a + b - c)$$

**Sol.** (i)  $(x^2 - 5)(x + 5) + 25$

$$\begin{aligned} &= x^2(x + 5) + 5(x + 5) + 25 \\ &= x^3 + 5x^2 - 5x - 25 + 25 \\ &= x^3 + 5x^2 - 5x + 0 = x^3 + 5x^2 - 5x \end{aligned}$$

$$\begin{aligned} \text{(ii)} \quad & (a^2 + 5)(b^3 + 3) + 5 \\ &= a^2(b^3 + 3) + 5(b^3 + 3) + 5 \\ &= a^2b^3 + 3a^2 + 5b^3 + 15 + 5 \\ &= a^2b^3 + 3a^2 + 5b^3 + 20 \end{aligned}$$

$$\begin{aligned} \text{(iii)} \quad & (t + s^2)(t^2 - s) \\ &= t(t^2 - s) + s^2(t^2 - s) \\ &= t^3 - st + s^2t^2 - s^3 \\ &= t^3 + s^2t^2 - st - s^3 \end{aligned}$$

$$\begin{aligned} \text{(iv)} \quad & (a + b)(c - d) + (a - b)(c + d) + 2(ac + bd) \\ &= a(c - d) + b(c - d) + a(c + d) \\ &\quad - b(c + d) + 2ac + 2bd \\ &= ac - ad + bc - bd + ac + ad \\ &\quad - bc - bd + 2ac + 2bd \\ &= ac + ac + 2ac + bc - bc - ad \\ &\quad + ad - bd - bd + 2bd \\ &= 4ac + 0 + 0 + 0 \\ &= 4ac \end{aligned}$$

$$\begin{aligned} \text{(v)} \quad & (x + y)(2x + y) + (x + 2y)(x - y) \\ &= x(2x + y) + y(2x + y) + x(x - y) \\ &\quad + 2y(x - y) \\ &= 2x^2 + xy + 2xy + y^2 + x^2 - xy \\ &\quad + 2xy - 2y^2 \end{aligned}$$

$$\begin{aligned} &= 2x^2 + x^2 + xy + 2xy - xy \\ &\quad + 2xy + y^2 - 2y^2 \\ &= 3x^2 + 4xy - y^2 \end{aligned}$$

$$\begin{aligned} \text{(vi)} \quad & (x + y)(x^2 - xy + y^2) \\ &= x(x^2 - xy + y^2) + y(x^2 - xy + y^2) \\ &= x^3 - x^2y + xy^2 + x^2y - xy^2 + y^3 \\ &= x^3 - x^2y + x^2y + xy^2 - xy^2 + y^3 \\ &= x^3 - 0 + 0 + y^3 \\ &= x^3 + y^3 \end{aligned}$$

$$\begin{aligned} \text{(vii)} \quad & (1.5x - 4y)(1.5x + 4y + 3) - 4.5x + 12y \\ &= 1.5x(1.5x + 4y + 3) - 4y(1.5x \\ &\quad + 4y + 3) - 4.5x + 12y \\ &= 2.25x^2 + 6xy + 4.5x - 6xy \\ &\quad - 16y^2 - 12y - 4.5x + 12y \\ &= 2.25x^2 + 6xy - 6xy + 4.5x \\ &\quad - 4.5x + 12y - 12y - 16y^2 \\ &= 2.25x^2 + 0 + 0 + 0 - 16y^2 \\ &= 2.25x^2 - 16y^2 \end{aligned}$$

$$\begin{aligned} \text{(viii)} \quad & (a + b + c)(a + b - c) \\ &= a(a + b - c) + b(a + b - c) \\ &\quad + c(a + b - c) \\ &= a^2 + ab - ac + ab + b^2 - bc \\ &\quad + ac + bc - c^2 \\ &= a^2 + ab + ab - bc + bc - ac \\ &\quad + ac + b^2 - c^2 \\ &= a^2 + 2ab + b^2 - c^2 + 0 + 0 \\ &= a^2 + 2ab + b^2 - c^2 \end{aligned}$$

**TRY THESE (PAGE 149)**

**Q1.** Put  $-b$  in place of  $b$  in identity (I). Do you get identity (II)?

$$\text{Sol.} \quad (a + b)^2 = a^2 + 2ab + b^2$$

$$\Rightarrow (a - b)^2 = a^2 + 2a(-b) + (-b)^2 = a^2 - 2a + b^2$$

Yes, we get identity II.

**TRY THESE (PAGE 149)**

**Q1.** Verify Identity (IV), for  $a = 2, b = 3, x = 5$ .

**Sol.** We have  $(x + a)(x + b)$

$$= x^2 + (a + b)x + ab$$

$$\text{LHS} = (x + a)(x + b)$$

$$= (5 + 2)(5 + 3)$$

$$= (7)(8) = 56$$

$$\text{RHS} = x^2 + (a + b)x + ab$$

$$= (5)^2 + (2 + 3)(5) + (2)(3)$$

$$= 25 + 5 \times 5 + 6$$

$$= 25 + 25 + 6 = 56$$

$$\text{LHS} = \text{RHS}$$

Hence, verified.

**Q2.** Consider, the special case of Identity (IV) with  $a = b$ , what do you get? Is it related to Identity (I)?

**Sol.** We have  $(x + a)(x + b) = x^2 + (a + b)x + ab$

Special case, when  $a = b$ , we get

$$(x + a)(x + a) = x^2 + (a + a)x + a \cdot a$$

$$(x + a)^2 = x^2 + 2ax + a^2$$

which is the formula of  $(a + b)^2 = a^2 + 2ab + b^2$

Yes, it is related to identity (I).

**Q3.** Consider, the special case of Identity (IV) with  $a = -c$  and  $b = -c$ . What do you get? Is it related to Identity (II)?

**Sol.** We have  $(x + a)(x + b) = x^2 + (a + b)x + ab$

Special case, put  $a = -c$  and  $b = -c$

$$(x - c)(x - c) = x^2 + (-c - c)x + (-c)(-c)$$

$$(x - c)^2 = x^2 - 2cx + c^2$$

which is the formula of

$$(a - b)^2 = a^2 - 2ab + b^2$$

Yes, it is related to Identity (II).

**Q4.** Consider the special case of Identity (IV) with  $b = -a$ . What do you get? Is it related to Identity (III)?

**Sol.** We have  $(x + a)(x + b)$

$$= x^2 + (a + b)x + ab$$

Special case, put  $b = -a$

$$(x + a)(x - a) = x^2 + (a - a)x + a(-a)$$

$$\Rightarrow (x + a)(x - a) = x^2 + 0 - a^2$$

$$\Rightarrow (x + a)(x - a) = x^2 - a^2$$

which is the formula of

$$(a - b)(a + b) = a^2 - b^2$$

Yes, it is related to Identity (iii).

### EXERCISE 9.5

**Q1.** Use a suitable identity to get each of the following products:

(i)  $(x + 3)(x + 3)$

(ii)  $(2y + 5)(2y + 5)$

(iii)  $(2a - 7)(2a - 7)$

(iv)  $\left(3a - \frac{1}{2}\right)\left(3a - \frac{1}{2}\right)$

(v)  $(1.1m - 0.4)(1.1m + 0.4)$

(vi)  $(a^2 + b^2)(-a^2 + b^2)$

(vii)  $(6x - 7)(6x + 7)$

(viii)  $(-a + c)(-a + c)$

(ix)  $\left(\frac{x}{2} + \frac{3y}{4}\right)\left(\frac{x}{2} + \frac{3y}{4}\right)$

(x)  $(7a - 9b)(7a - 9b)$

**Sol.** (i)  $(x + 3)(x + 3)$

$$= (x + 3)^2$$

$$= (x)^2 + 2 \times x \times 3 + (3)^2$$

$$= x^2 + 6x + 9 \quad [(a + b)^2 = a^2 + 2ab + b^2]$$

(ii)  $(2y + 5)(2y + 5)$

$$= (2y + 5)^2$$

$$= (2y)^2 + 2(2y)(5) + (5)^2$$

$$[(a + b)^2 = a^2 + 2ab + b^2]$$

$$= 4y^2 + 20y + 25$$

(iii)  $(2a - 7)(2a - 7)$

$$= (2a - 7)^2$$

$$= (2a)^2 - 2(2a)(7) + (7)^2$$

$$[(a - b)^2 = a^2 - 2ab + b^2]$$

$$= 4a^2 - 28a + 49$$

(iv)  $\left(3a - \frac{1}{2}\right)\left(3a - \frac{1}{2}\right)$

$$= \left(3a - \frac{1}{2}\right)^2$$

$$= (3a)^2 - 2(3a)\left(\frac{1}{2}\right) + \left(\frac{1}{2}\right)^2$$

$$[(a - b)^2 = a^2 - 2ab + b^2]$$

$$= 9a^2 - 3a + \frac{1}{4}$$

(v)  $(1.1m - 0.4)(1.1m + 0.4)$

$$= (1.1m)^2 - (0.4)^2$$

$$[(a + b)(a - b) = a^2 - b^2]$$

$$= 1.21m^2 - 0.16$$

(vi)  $(a^2 + b^2)(-a^2 + b^2)$

$$= (b^2 + a^2)(b^2 - a^2)$$

$$= (b^2)^2 - (a^2)^2 \quad [(a + b)(a - b) = a^2 - b^2]$$

$$= b^4 - a^4$$

$$= -a^4 + b^4$$

(vii)  $(6x - 7)(6x + 7)$

$$= (6x)^2 - (7)^2 \quad [(a + b)(a - b) = a^2 - b^2]$$

$$= 36x^2 - 49$$

(viii)  $(-a + c)(-a + c)$

$$= [(-a) + c]^2$$

$$= (-a)^2 - 2ac + c^2$$

$$= a^2 - 2ac + c^2 \quad [(a - b)^2 = a^2 - 2ab + b^2]$$

$$\begin{aligned}
 \text{(ix)} \quad & \left(\frac{x}{2} + \frac{3y}{4}\right)\left(\frac{x}{2} + \frac{3y}{4}\right) \\
 &= \left(\frac{x}{2} + \frac{3y}{4}\right)^2 \\
 &= \left(\frac{x}{2}\right)^2 + 2\left(\frac{x}{2}\right)\left(\frac{3y}{4}\right) + \left(\frac{3y}{4}\right)^2 \\
 & \quad \quad \quad [(a+b)^2 = a^2 + 2ab + b^2] \\
 &= \frac{x^2}{4} + \frac{3}{4}xy + \frac{9y^2}{16}
 \end{aligned}$$

$$\begin{aligned}
 \text{(x)} \quad & (7a - 9b)(7a - 9b) \\
 &= (7a)^2 - 2(7a)(9b) + (9b)^2 \\
 & \quad \quad \quad [(a-b)^2 = a^2 - 2ab + b^2] \\
 &= 49a^2 - 126ab + 81b^2
 \end{aligned}$$

**Q2.** Use the identity  $(x+a)(x+b) = x^2 + (a+b)x + ab$  to find the following products.

$$\text{(i)} \quad (x+3)(x+7)$$

$$\text{(ii)} \quad (4x+5)(4x+1)$$

$$\text{(iii)} \quad (4x-5)(4x-1)$$

$$\text{(iv)} \quad (4x+5)(4x-1)$$

$$\text{(v)} \quad (2x+5y)(2x+3y)$$

$$\text{(vi)} \quad (2a^2+9)(2a^2+5)$$

$$\text{(vii)} \quad (xyz-4)(xyz-2)$$

**Sol.** (i)  $(x+3)(x+7)$

$$= x^2 + (3+7)x + 3 \times 7$$

$$= x^2 + 10x + 21$$

(ii)  $(4x+5)(4x+1)$

$$= (4x)^2 + (5+1)(4x) + 5 \times 1$$

$$= 16x^2 + 6(4x) + 5$$

$$= 16x^2 + 24x + 5$$

(iii)  $(4x-5)(4x-1)$

$$= (4x)^2 - (5+1)(4x) + (-5) \times (-1)$$

$$= 16x^2 - 6(4x) + 5$$

$$= 16x^2 - 24x + 5$$

(iv)  $(4x+5)(4x-1)$

$$= (4x)^2 + (5-1)(4x) + 5 \times (-1)$$

$$= 16x^2 + 4(4x) - 5$$

$$= 16x^2 + 16x - 5$$

(v)  $(2x+5y)(2x+3y)$

$$= (2x)^2 + (5y+3y)(2x) + (5y)(3y)$$

$$= 4x^2 + (8y)(2x) + 15y^2$$

$$= 4x^2 + 16xy + 15y^2$$

(vi)  $(2a^2+9)(2a^2+5)$

$$= (2a^2)^2 + (9+5)(2a^2) + 9 \times 5$$

$$= 4a^4 + (14)(2a^2) + 45$$

$$= 4a^4 + 28a^2 + 45$$

(vii)  $(xyz-4)(xyz-2)$

$$= (xyz)^2 - (4+2)(xyz) + (-4)(-2)$$

$$= x^2y^2z^2 - (6)(xyz) + 8$$

$$= x^2y^2z^2 - 6xyz + 8$$

**Q3.** Find the following squares by using the identities.

$$\text{(i)} \quad (b-7)^2 \quad \text{(ii)} \quad (xy+3z)^2$$

$$\text{(iii)} \quad (6x^2-5y)^2 \quad \text{(iv)} \quad \left(\frac{2}{3}m + \frac{3}{2}n\right)^2$$

$$\text{(v)} \quad (0.4p-0.5q)^2 \quad \text{(vi)} \quad (2xy+5y)^2$$

**Sol.** (i)  $(b-7)^2 = (b)^2 - 2(b)(7) + (7)^2$   
 $= b^2 - 14b + 49$

$$\text{[using } (a-b)^2 = a^2 - 2ab + b^2]$$

(ii)  $(xy+3z)^2$

$$= (xy)^2 + 2(xy)(3z) + (3z)^2$$

$$\text{[using } (a+b)^2 = a^2 + 2ab + b^2]$$

$$= x^2y^2 + 6xyz + 9y^2$$

(iii)  $(6x^2-5y)^2$

$$= (6x^2)^2 - 2(6x^2)(5y) + (5y)^2$$

$$\text{[using } (a-b)^2 = a^2 - 2ab + b^2]$$

$$= 36x^4 - 60x^2y + 25y^2$$

(iv)  $\left(\frac{2}{3}m + \frac{3}{2}n\right)^2$

$$= \left(\frac{2}{3}m\right)^2 + 2\left(\frac{2}{3}m\right)\left(\frac{3}{2}n\right) + \left(\frac{3}{2}n\right)^2$$

$$\text{[using } (a+b)^2 = a^2 + 2ab + b^2]$$

$$= \frac{4}{9}m^2 + 2mn + \frac{9}{4}n^2$$

(v)  $(0.4p-0.5q)^2$

$$= (0.4p)^2 - 2(0.4p)(0.5q) + (0.5q)^2$$

$$\text{[using } (a-b)^2 = a^2 - 2ab + b^2]$$

$$= 0.16p^2 - 0.4pq + 0.25q^2$$

(vi)  $(2xy+5y)^2$

$$= (2xy)^2 + 2(2xy)(5y) + (5y)^2$$

$$\text{[using } (a+b)^2 = a^2 + 2ab + b^2]$$

$$= 4x^2y^2 + 20xy^2 + 25y^2$$

**Q4** Simplify:

$$\text{(i)} \quad (a^2-b^2)^2$$

$$\text{(ii)} \quad (2x+5)^2 - (2x-5)^2$$

$$\text{(iii)} \quad (7m-8n)^2 + (7m+8n)^2$$

$$\text{(iv)} \quad (4m+5n)^2 + (5m+4n)^2$$

$$\text{(v)} \quad (2.5p-1.5q)^2 - (1.5p-2.5q)^2$$

$$\text{(vi)} \quad (ab+bc)^2 - 2ab^2c$$

$$\text{(vii)} \quad (m^2-n^2m)^2 + 2m^3n^2$$

**Sol.** (i)  $(a^2-b^2)^2$

$$= (a^2)^2 - 2a^2b^2 + (b^2)^2$$

$$= a^4 - 2a^2b^2 + b^4$$

$$\text{[using } (a-b)^2 = a^2 - 2ab + b^2]$$

$$\begin{aligned}
 \text{(ii)} \quad & (2x + 5)^2 - (2x - 5)^2 \\
 & = [(2x)^2 + 2(2x)(5) + (5)^2] - [(2x)^2 \\
 & \quad - 2(2x)(5) + (5)^2] \\
 & = (4x^2 + 20x + 25) - (4x^2 - 20x + 25) \\
 & = \cancel{4x^2} + 20x + \cancel{25} - \cancel{4x^2} + 20x - \cancel{25} \\
 & = 20x + 20x = 40x
 \end{aligned}$$

**Alternately:**

$$\begin{aligned}
 & (2x + 5)^2 - (2x - 5)^2 \\
 & = [(2x + 5) + (2x - 5)] [(2x + 5) - (2x - 5)] \\
 & \quad \text{[using } a^2 - b^2 = (a + b)(a - b)\text{]} \\
 & = (2x + \cancel{5} + 2x - \cancel{5}) (\cancel{2x} + 5 - \cancel{2x} + 5) \\
 & = (2x + 2x)(5 + 5) \\
 & = 4x \times 10 = 40x
 \end{aligned}$$

$$\begin{aligned}
 \text{(iii)} \quad & (7m - 8n)^2 + (7m + 8n)^2 \\
 & = (7m)^2 - 2(7m)(8n) + (8n)^2 + (7m)^2 \\
 & \quad + 2(7m)(8n) + (8n)^2 \\
 & = 49m^2 - \cancel{112mn} + 64n^2 + 49m^2 \\
 & \quad + \cancel{112mn} + 64n^2 \\
 & = 98m^2 + 128n^2
 \end{aligned}$$

$$\begin{aligned}
 \text{(iv)} \quad & (4m + 5n)^2 + (5m + 4n)^2 \\
 & = (4m)^2 + 2(4m)(5n) + (5n)^2 \\
 & \quad + (5m)^2 + 2(5m)(4n) + (4n)^2 \\
 & = 16m^2 + 40mn + 25n^2 + 25m^2 \\
 & \quad + 40mn + 16n^2 \\
 & = 41m^2 + 80mn + 41n^2
 \end{aligned}$$

$$\begin{aligned}
 \text{(v)} \quad & (2.5p - 1.5q)^2 - (1.5p - 2.5q)^2 \\
 & = [(2.5p)^2 - 2(2.5p)(1.5q) + (1.5q)^2] \\
 & \quad - [(1.5p)^2 - 2(1.5p)(2.5q) + (2.5q)^2] \\
 & = (6.25p^2 - 7.5pq + 2.25q^2) \\
 & \quad - (2.25p^2 - 7.5pq + 6.25q^2) \\
 & = 6.25p^2 - \cancel{7.5pq} + 2.25q^2 \\
 & \quad - 2.25p^2 + \cancel{7.5pq} - 6.25q^2 \\
 & = 6.25p^2 - 2.25p^2 + 2.25q^2 - 6.25q^2 \\
 & = 4p^2 - 4q^2
 \end{aligned}$$

$$\begin{aligned}
 \text{(vi)} \quad & (ab + bc)^2 - 2ab^2c \\
 & = (ab)^2 + 2(ab)(bc) + (bc)^2 - 2ab^2c \\
 & = a^2b^2 + \cancel{2ab^2c} + b^2c^2 - \cancel{2ab^2c} \\
 & = a^2b^2 + b^2c^2
 \end{aligned}$$

$$\begin{aligned}
 \text{(vii)} \quad & (m^2 - n^2m)^2 + 2m^3n^2 \\
 & = (m^2)^2 - 2m^2(n^2m) + (n^2m)^2 + 2m^3n^2 \\
 & = m^4 - \cancel{2m^3n^2} + n^4m^2 + \cancel{2m^3n^2} \\
 & = m^4 + n^4m^2
 \end{aligned}$$

**Q5. Show that:**

$$\text{(i)} \quad (3x + 7)^2 - 84x = (3x - 7)^2$$

$$\text{(ii)} \quad (9p - 5q)^2 + 180pq = (9p + 5q)^2$$

$$\text{(iii)} \quad \left(\frac{4}{3}m - \frac{3}{4}n\right)^2 + 2mn = \frac{16}{9}m^2 + \frac{9}{16}n^2$$

$$\text{(iv)} \quad (4pq + 3q)^2 - (4pq - 3q)^2 = 48pq^2$$

$$\text{(v)} \quad (a - b)(a + b) + (b - c)(b + c) + (c - a)(c + a) = 0$$

**Sol.** (i) To Show that:

$$\begin{aligned}
 & (3x + 7)^2 - 84x = (3x - 7)^2 \\
 \text{LHS} & = (3x + 7)^2 - 84x \\
 & = (3x)^2 + 2(3x)(7) + (7)^2 - 84x \\
 & = 9x^2 + 42x + 49 - 84x \\
 & = 9x^2 - 42x + 49 \\
 & = (3x)^2 - 2(3x)(7) + (7)^2 \\
 & = (3x - 7)^2 = \text{RHS}
 \end{aligned}$$

$$\text{LHS} = \text{RHS}$$

Hence, proved.

(ii) To show that:

$$\begin{aligned}
 & (9p - 5q)^2 + 180pq = (9p + 5q)^2 \\
 \text{LHS} & = (9p - 5q)^2 + 180pq \\
 & = (9p)^2 - 2(9p)(5q) + (5q)^2 + 180pq \\
 & = 81p^2 - 90pq + 25q^2 + 180pq \\
 & = 81p^2 + 90pq + 25q^2 \\
 & = (9p)^2 + 2(9p)(5q) + (5q)^2 \\
 & = (9p + 5q)^2 = \text{RHS}
 \end{aligned}$$

$$\text{LHS} = \text{RHS}$$

Hence, proved.

(iii) To show that:

$$\left(\frac{4}{3}m - \frac{3}{4}n\right)^2 + 2mn = \frac{16}{9}m^2 + \frac{9}{16}n^2$$

$$\text{LHS} = \left(\frac{4}{3}m - \frac{3}{4}n\right)^2 + 2mn$$

$$= \left(\frac{4}{3}m\right)^2 - 2\left(\frac{4}{3}m\right)\left(\frac{3}{4}n\right) + \left(\frac{3}{4}n\right)^2 + 2mn$$

$$= \frac{16}{9}m^2 - \cancel{2mn} + \frac{9}{16}n^2 + \cancel{2mn}$$

$$= \frac{16}{9}m^2 + \frac{9}{16}n^2 = \text{RHS}$$

$$\text{LHS} = \text{RHS}$$

Hence, proved.

(iv) To show that:

$$(4pq + 3q)^2 - (4pq - 3q)^2 = 48pq^2$$

$$\text{LHS} = (4pq + 3q)^2 - (4pq - 3q)^2$$

$$= [(4pq + 3q) + (4pq - 3q)]$$

$$[(4pq + 3q) - (4pq - 3q)]$$

$$\begin{aligned}
 &= (4pq + \cancel{3q} + 4pq - \cancel{3q}) \\
 &\quad (\cancel{4pq} + 3q - \cancel{4pq} + 3q) \\
 &= (8pq)(6q) \\
 &= 48pq^2 = \text{RHS}
 \end{aligned}$$

LHS = RHS

Hence, proved.

(v) To show that:

$$(a-b)(a+b) + (b-c)(b+c)(c-a)(c+a) = 0$$

$$\begin{aligned}
 \text{LHS} &= (a^2 - b^2) + (b^2 - c^2) + (c^2 - a^2) \\
 &\quad [\because (x+y)(x-y) = x^2 - y^2]
 \end{aligned}$$

$$\begin{aligned}
 &= \cancel{a^2} - \cancel{b^2} + \cancel{b^2} - \cancel{c^2} + \cancel{c^2} - \cancel{a^2} \\
 &= 0 = \text{RHS}
 \end{aligned}$$

LHS = RHS

Hence, proved.

Q6. Using identities, evaluate:

- (i)  $71^2$                       (ii)  $99^2$   
 (iii)  $102^2$                     (iv)  $998^2$   
 (v)  $5.2^2$                       (vi)  $297 \times 303$   
 (vii)  $78 \times 82$                 (viii)  $8.9^2$   
 (ix)  $1.05 \times 9.5$

Sol. (i)  $71^2 = (70 + 1)^2$   
 $= (70)^2 + 2(70)(1) + (1)^2$   
 $\quad [(a+b)^2 = a^2 + 2ab + b^2]$   
 $= 4900 + 140 + 1$   
 $= 5041$

Hence,  $71^2 = 5041$ 

(ii)  $99^2 = (100 - 1)^2$   
 $= (100)^2 - 2(100)(1) + (1)^2$   
 $\quad [(a-b)^2 = a^2 - 2ab + b^2]$   
 $= 10000 - 200 + 1$   
 $= 10001 - 200$   
 $= 9801$

Hence,  $99^2 = 9801$ 

(iii)  $102^2 = (100 + 2)^2$   
 $= (100)^2 + 2(100)(2) + (2)^2$   
 $\quad [(a+b)^2 = a^2 + 2ab + b^2]$   
 $= 10000 + 400 + 4$   
 $= 10404$

Hence,  $102^2 = 10404$ 

(iv)  $998^2 = (1000 - 2)^2$   
 $= (1000)^2 - 2(1000)(2) + (2)^2$   
 $\quad [(a-b)^2 = a^2 - 2ab + b^2]$   
 $= 1000000 - 4000 + 4$   
 $= 1000004 - 4000$   
 $= 996004$

Hence,  $998^2 = 996004$ 

(v)  $5.2^2 = (5 + 0.2)^2$   
 $= (5)^2 + 2(5)(0.2) + (0.2)^2$   
 $\quad [(a+b)^2 = a^2 + 2ab + b^2]$   
 $= 25 + 2 + 0.04$   
 $= 27 + 0.04$   
 $= 27.04$

Hence,  $(5.2)^2 = 27.04$ 

(vi)  $297 \times 303 = (300 - 3)(300 + 3)$   
 $= (300)^2 - (3)^2 \quad [(a+b)(a-b) = a^2 - b^2]$   
 $= 90000 - 9$   
 $= 89991$

Hence,  $297 \times 303 = 89991$ 

(vii)  $78 \times 82 = (80 - 2)(80 + 2)$   
 $= (80)^2 - (2)^2 \quad [(a+b)(a-b) = a^2 - b^2]$   
 $= 6400 - 4$   
 $= 6396$

Hence,  $78 \times 82 = 6396$ 

(viii)  $8.9^2 = (9 - 0.1)^2$   
 $= (9)^2 - 2(9)(0.1) + (0.1)^2$   
 $\quad [(a-b)^2 = a^2 - 2ab + b^2]$   
 $= 81 - 1.8 + 0.01$   
 $= 81.01 - 1.8$   
 $= 79.21$

Hence,  $8.9^2 = 79.21$ 

(ix)  $1.05 \times 9.5 = (1 + 0.5)(10 - 0.5)$   
 $= 1(10 - 0.5) + 0.05(10 - 0.5)$   
 $= 10 - 0.5 + 0.05 \times 10 - 0.05 \times 0.5$   
 $= 10 - 0.5 + 0.5 - 0.025$   
 $= 10.5 - 0.525$   
 $= 9.975$

Hence,  $1.05 \times 9.5 = 9.975$ Q.7. Using  $a^2 - b^2 = (a+b)(a-b)$ , find

- (i)  $51^2 - 49^2$                 (ii)  $(1.02)^2 - (0.98)^2$   
 (iii)  $153^2 - 147^2$             (iv)  $12.1^2 - 7.9^2$

Sol. (i)  $51^2 - 49^2 = (51 + 49)(51 - 49)$   
 $= 100 \times 2 = 200$   
 (ii)  $(1.02)^2 - (0.98)^2$   
 $= (1.02 + 0.98)(1.02 - 0.98)$   
 $= 2.00 \times 0.04$   
 $= 0.08$

(iii)  $153^2 - 147^2$   
 $= (153 + 147)(153 - 147)$   
 $= 300 \times 6 = 1800$

(iv)  $12.1^2 - 7.9^2$   
 $= (12.1 + 7.9)(12.1 - 7.9)$   
 $= 20.0 \times 4.2 = 84$

Q8. Using  $(x + a)(x + b) = x^2 + (a + b)x + ab$ , find

(i)  $103 \times 104$

(ii)  $5.1 \times 5.2$

(iii)  $103 \times 98$

(iv)  $9.7 \times 9.8$

Sol. (i)  $103 \times 104$

$$= (100 + 3)(100 + 4)$$

$$= (100)^2 + (3 + 4)(100) + 3 \times 4$$

$$= 10000 + 700 + 12 = 10712$$

(ii)  $5.1 \times 5.2$

$$= (5 + 0.1)(5 + 0.2)$$

$$= (5)^2 + (0.1 + 0.2)(5) + 0.1 \times 0.2$$

$$= 25 + 1.5 + 0.02 = 26.5 + 0.02$$

$$= 26.52$$

(iii)  $103 \times 98$

$$= (100 + 3)(100 - 2)$$

$$= (100)^2 + (3 - 2)(100) + 3 \times (-2)$$

$$= 10000 + 100 - 6$$

$$= 10100 - 6 = 10094$$

(iv)  $9.7 \times 9.8$

$$= (10 - 0.3)(10 - 0.2)$$

$$= (10)^2 - (0.3 + 0.2)(10) + (-0.3)(-0.2)$$

$$= 100 - 5 + 0.06$$

$$= 95 + 0.06$$

$$= 95.06$$

## Learning More Q & A

### I. VERY SHORT ANSWER (VSA) QUESTIONS

Q1. Write two examples of each of

(i) Monomials

(ii) Binomials

(iii) Trinomials

Sol. (i) Monomials:

(a)  $3x$

(b)  $5xy^2$

(ii) Binomials: (a)  $p + q$  (b)  $-5a + 2b$

(iii) Trinomials:

(a)  $a + b + c$  (b)  $x^2 + x + 2$

Q2. Identify the like expressions.

$5x, -14x, 3x^2 + 1, x^2, -9x^2, xy, -3xy$

Like terms:  $5x$  and  $-14x$ ,  $x^2$  and  $-9x^2$ ,  $xy$  and  $-3xy$

Q3. Identify the terms and their coefficients for each of the following expressions:

(i)  $3x^2y - 5x$

(ii)  $xyz - 2y$

(iii)  $-x - x^2$

Sol. (i) Terms

Coefficients

$3x^2y$

3

$-5x$

-5

(ii)  $xyz$

1

$-2y$

-2

(iii)  $-x$

-1

$-x^2$

-1

Q4. Add:  $-3a^2b^2, -\frac{5}{2}a^2b^2, 4a^2b^2, \frac{2}{3}a^2b^2$

Sol.  $(-3a^2b^2) + \left(-\frac{5}{2}a^2b^2\right) + (4a^2b^2) + \left(\frac{2}{3}a^2b^2\right)$

$$= \left(-3 - \frac{5}{2} + 4 + \frac{2}{3}\right)a^2b^2$$

$$= \left(\frac{-18 - 15 + 24 + 4}{6}\right)a^2b^2$$

$$= \frac{5}{6}a^2b^2$$

Q5. Add:  $8x^2 + 7xy - 6y^2, 4x^2 - 3xy + 2y^2$  and  $-4x^2 + xy - y^2$

Sol.

$$8x^2 + 7xy - 6y^2$$

$$4x^2 - 3xy + 2y^2$$

$$-4x^2 + xy - y^2$$

+

Sum  $8x^2 + 5xy - 5y^2$

Q6. Subtract:  $(4x + 5)$  from  $(-3x + 7)$

Sol.  $(-3x + 7) - (4x + 5)$

$$= -3x + 7 - 4x - 5$$

$$= -3x - 4x + 7 - 5$$

$$= -7x + 2$$

Q7. Subtract:  $3x^2 - 5x + 7$  from  $5x^2 - 7x + 9$

Sol.  $(5x^2 - 7x + 9) - (3x^2 - 5x + 7)$

$$= 5x^2 - 7x + 9 - 3x^2 + 5x - 7$$

$$= 5x^2 - 3x^2 + 5x - 7x + 9 - 7$$

$$= 2x^2 - 2x + 2$$

Q8. Multiply the following expressions:

(a)  $3xy^2 \times (-5x^2y)$

(b)  $\frac{1}{2}x^2yz \times \frac{2}{3}xy^2z \times \frac{1}{5}x^2yz$

Sol. (a)  $3xy^2 \times (-5x^2y)$

$$= (3) \times (-5) \cdot x^3y^3$$

$$= -15x^3y^3$$

(b)  $\frac{1}{2}x^2yz \times \frac{2}{3}xy^2z \times \frac{1}{5}x^2yz$

$$= \left(\frac{1}{2} \times \frac{2}{3} \times \frac{1}{5}\right) \cdot x^2yz \times xy^2z \times x^2yz$$

$$= \frac{1}{15}x^5y^4z^3$$

**Q9.** Find the area of the rectangle whose length and breadths are  $3x^2y$  m and  $5xy^2$  m respectively.

**Sol.** Length =  $3x^2y$  m, breadth =  $5xy^2$  m  
 Area of rectangle = Length  $\times$  Breadth  
 $= (3x^2y \times 5xy^2)$  sq m  
 $= (3 \times 5) \times x^2y \times xy^2$  sq m  
 $= 15x^3y^3$  sq m

**Q10.** Multiply  $x^2 + 7x - 8$  by  $-2y$ .

**Sol.**

$$\begin{array}{r} x^2 + 7x - 8 \\ \times -2y \\ \hline -2x^2y - 14xy + 16y \end{array}$$

## II. SHORT ANSWER (SA) QUESTIONS

**Q11.** Simplify the following:

(i)  $a^2(b^2 - c^2) + b^2(c^2 - a^2) + c^2(a^2 - b^2)$

(ii)  $x^2(x - 3y^2) - xy(y^2 - 2xy) - x(y^3 - 5x^2)$

**Sol.** (i)  $a^2(b^2 - c^2) + b^2(c^2 - a^2) + c^2(a^2 - b^2)$   
 $= \cancel{a^2b^2} - \cancel{a^2c^2} + \cancel{b^2c^2}$   
 $\quad - \cancel{b^2a^2} + \cancel{c^2a^2} - \cancel{c^2b^2}$   
 $= 0$

(ii)  $x^2(x - 3y^2) - xy(y^2 - 2xy) - x(y^3 - 5x^2)$   
 $= x^3 - 3x^2y^2 - xy^3 + 2x^2y^2 - xy^3 + 5x^3$   
 $= x^3 + 5x^3 - 3x^2y^2 + 2x^2y^2 - xy^3 - xy^3$   
 $= 6x^3 - x^2y^2 - 2xy^3$

**Q12.** Multiply  $(3x^2 + 5y^2)$  by  $(5x^2 - 3y^2)$

**Sol.**  $(3x^2 + 5y^2) \times (5x^2 - 3y^2)$   
 $= 3x^2(5x^2 - 3y^2) + 5y^2(5x^2 - 3y^2)$   
 $= 15x^4 - 9x^2y^2 + 25x^2y^2 - 15y^4$   
 $= 15x^4 + 16x^2y^2 - 15y^4$

**Q13.** Multiply  $(6x^2 - 5x + 3)$  by  $(3x^2 + 7x - 3)$

**Sol.**  $(6x^2 - 5x + 3) \times (3x^2 + 7x - 3)$   
 $= 6x^2(3x^2 + 7x - 3) - 5x(3x^2 + 7x - 3)$   
 $\quad + 3(3x^2 + 7x - 3)$   
 $= 18x^4 + 42x^3 - 18x^2 - 15x^3 - 35x^2 + 15x$   
 $\quad + 9x^2 + 21x - 9$   
 $= 18x^4 + 42x^3 - 15x^3 - 18x^2 - 35x^2 + 9x^2$   
 $\quad + 15x + 21x - 9$   
 $= 18x^4 + 27x^3 - 44x^2 + 36x - 9$

**Q14.** Simplify:

$2x^2(x + 2) - 3x(x^2 - 3) - 5x(x + 5)$

**Sol.**  $2x^2(x + 2) - 3x(x^2 - 3) - 5x(x + 5)$   
 $= 2x^3 + 4x^2 - 3x^3 + 9x - 5x^2 - 25x$   
 $= 2x^3 - 3x^3 - 5x^2 + 4x^2 + 9x - 25x$   
 $= -x^3 - x^2 - 16x$

**Q15.** Multiply  $x^2 + 2y$  by  $x^3 - 2xy + y^3$  and find the value of the product for  $x = 1$  and  $y = -1$ .

**Sol.**  $(x^2 + 2y) \times (x^3 - 2xy + y^3)$   
 $= x^2(x^3 - 2xy + y^3) + 2y(x^3 - 2xy + y^3)$   
 $= x^5 - \cancel{2x^3y} + x^2y^3 + \cancel{2x^3y} - 4xy^2 + 2y^4$   
 $= x^5 + x^2y^3 - 4xy^2 + 2y^4$

Put  $x = 1$  and  $y = -1$

$= (1)^5 + (1)^2(-1)^3 - 4(1)(-1)^2 + 2(-1)^4$   
 $= 1 + (1)(-1) - 4(1)(1) + 2(1)$   
 $= 1 - 1 - 4 + 2$   
 $= -2$

**Q16.** Using suitable identity find:

(i)  $48^2$  (NCERT Exemplar) (ii)  $96^2$

(iii)  $231^2 - 131^2$  (iv)  $97 \times 103$

(v)  $181^2 - 19^2 = 162 \times 200$  (NCERT Exemplar)

**Sol.** (i)  $(50 - 2)^2 = (50)^2 - 2 \times 50 \times 2 + (2)^2$   
 $= 2500 - 200 + 4$   
 $= 2504 - 200$   
 $= 2304$

(ii)  $96^2 = (100 - 4)^2$   
 $= (100)^2 - 2(100)(4) + (4)^2$   
 $\quad [\because (a - b)^2 = a^2 - 2ab + b^2]$   
 $= 10000 - 800 + 16$   
 $= 10016 - 800$   
 $= 9216$

(iii)  $231^2 - 131^2$   
 $= (231 - 131)(231 + 131)$   
 $= (100)(362)$   
 $\quad [\because a^2 - b^2 = (a + b)(a - b)]$   
 $= 36200$

(iv)  $97 \times 103$   
 $= (100 - 3) \times (100 + 3)$   
 $= (100)^2 - (3)^2$   
 $\quad [(a + b)(a - b) = a^2 - b^2]$   
 $= 10000 - 9$   
 $= 9991$

(v)  $181^2 - 19^2 = (181 - 19)(181 + 19)$   
 $\quad [\text{Using } a^2 - b^2 = (a - b)(a + b)]$   
 $= 162 \times 200 = 32400$

**Q17.** If  $x^2 + \frac{1}{x^2} = 38$ , find the values of:

(i)  $x - \frac{1}{x}$  (ii)  $x^4 + \frac{1}{x^4}$

**Sol.** (i)  $\left(x - \frac{1}{x}\right)^2 = x^2 + \frac{1}{x^2} - 2 \times x \times \frac{1}{x}$   
 $\quad [\because (a - b)^2 = a^2 + b^2 - 2ab]$

$$= x^2 + \frac{1}{x^2} - 2$$

$$= 38 - 2 = 36$$

$$\therefore x - \frac{1}{x} = \sqrt{36} = 6$$

$$(ii) \left(x^2 + \frac{1}{x^2}\right)^2$$

$$= x^4 + \frac{1}{x^4} + 2 \times x^2 \times \frac{1}{x^2}$$

$$\Rightarrow (38)^2 = x^4 + \frac{1}{x^4} + 2$$

$$\left[ \text{Given } \left(x^2 + \frac{1}{x^2}\right) = 38 \right]$$

$$\Rightarrow 1444 - 2 = x^4 + \frac{1}{x^4}$$

$$\Rightarrow 1442 = x^4 + \frac{1}{x^4}$$

$$\therefore x^4 + \frac{1}{x^4} = 1442$$

Q18. Verify that  $(11pq + 4q)^2 - (11pq - 4q)^2 = 176pq^2$   
(NCERT Exemplar)

Sol. LHS =  $(11pq + 4q)^2 - (11pq - 4q)^2$   
 $= (11pq + 4q + 11pq - 4q) \times (11pq + 4q - 11pq + 4q)$   
 [using  $a^2 - b^2 = (a - b)(a + b)$ , here  $a = 11pq + 4q$  and  $b = 11pq - 4q$ ]

$$= (22pq)(8q) = 176pq^2$$

RHS. Hence Verified

Q19. Find the value of  $\frac{38^2 - 22^2}{16}$ , using a suitable identity. (NCERT Exemplar)

Sol. Since  $a^2 - b^2 = (a + b)(a - b)$ , therefore

$$38^2 - 22^2 = (38 - 22)(38 + 22)$$

$$= 16 \times 60$$

$$\text{So, } \frac{38^2 - 22^2}{16} = \frac{16 \times 60}{16}$$

$$= 60$$

Q20. Find the value of  $x$ , if

$$10000x = (9982)^2 - (18)^2 \quad (\text{NCERT Exemplar})$$

Sol. RHS =  $(9982)^2 - (18)^2$

$$= (9982 + 18)(9982 - 18)$$

$$[\text{Since } a^2 - b^2 = (a + b)(a - b)]$$

$$= (10000) \times (9964)$$

$$\text{LHS} = (10000) \times x$$

Comparing L.H.S. and RHS, we get

$$10000x = 10000 \times 9964$$

$$\text{or } x = \frac{10000 \times 9964}{10000} = 9964$$

## Test Yourself

Q1. Using the identities, find the values of the following:

(a)  $95 \times 105$

(b)  $995^2$

(NCERT Exemplar)

(c)  $47 \times 53$

(d)  $217^2 - 183^2$

(NCERT Exemplar)

Q2. Using identities, solve the following expressions:

(a)  $\left(\frac{1}{2}x - \frac{3}{2}y\right)^2$

(b)  $\left(2x - \frac{1}{x}\right)^2$

Q3. Multiply the following expressions:

(i)  $4xy$ ,  $5x^2y^2$  and  $6x^3y^3$     (ii)  $5x$  and  $-4xyz$

Q4. Add:  $4b(3b^2 + 5b - 7)$  and  $2(b^3 - 4b^2 + 5)$  and find the value for  $b = -1$ .

Q5. Simplify:  $(x + y)(2x - 3y + z) - (2x - 3y)z$

Q6. If  $x^2 + \frac{1}{x^2} = 27$ , find the values of

(i)  $x - \frac{1}{x}$

(ii)  $x^4 + \frac{1}{x^4}$

Q7. Using the identity  $(x + a)(x + b) = x^2 + (a + b)x + ab$ , find the values of

(i)  $(4x - 5)(2x - 6)$

(ii)  $(a^2 - 3)(a^2 + 5)$

Q8. If  $x + \frac{1}{x} = 3$ , find the value of

(a)  $x^2 + \frac{1}{x^2}$

(b)  $x^4 + \frac{1}{x^4}$

Q9. Simplify: (i)  $279 \times 279 - 21 \times 21$  (ii)  $91 \times 91 - 9 \times 9$  using the identities.

Q10. Find the value of  $x$  if

(i)  $13x = 58^2 - 45^2$

(ii)  $24x = 99^2 - 87^2$

Q11. Find the continued product:

(i)  $(x - 1)(x + 1)(x^2 + 1)$

(ii)  $(x + 3)(x - 3)(x^2 + 9)$

Q12. Simplify:

(i)  $1.62 \times 1.62 - 0.38 \times 0.38$

(ii)  $(203)^2 - (197)^2$



Q13. If  $x - y = 9$  and  $xy = 16$ , find the value of  $x^2 + y^2$ .

Q14. Find the value of  $16x^2 + 56x + 49$  if  $x = -1$ .

Q15. Find the value of

$$\frac{7.87 \times 7.87 - 1.72 \times 1.72}{6.15}$$

Q16. Find the values of the following:

(a)  $(a + b)^2 + (a - b)^2$

(b)  $(a + b)^2 - (a - b)^2$

Q17. Evaluate:  $\frac{5.43 \times 5.43 - 1.57 \times 1.57}{3.86}$

Q18. Simplify:  $\left(x^3 - \frac{1}{x^3}\right)\left(x^3 + \frac{1}{x^3}\right)\left(x^6 + \frac{1}{x^6}\right)$

### HIGHER ORDER THINKING SKILLS (HOTs) QUESTIONS

Q19. Simplify:  $\frac{4.359 \times 4.359 - 1.641 \times 1.641}{4.359 - 1.641}$

Q20. Simplify:

$$\frac{3.7 \times 3.7 + 2.3 \times 2.3 + 2 \times 3.7 \times 2.3}{4.6 \times 4.6 - 3.4 \times 3.4}$$

### ANSWERS

- |  |                                |
|--|--------------------------------|
| 1. (a) 9975  | (b) 990025                     |
| (c) 2491   | (d) 13600                      |
| 2. (a) $\frac{1}{4}x^2 + \frac{9}{4}y^2 - \frac{3}{2}xy$ | (b) $4x^2 + \frac{1}{x^2} - 4$ |
| 3. (i) $120x^6y^6$                                       | (ii) $-20x^2yz$                |
| 4. $14b^3 + 12b^2 - 28b + 10, 36$                        |                                |
| 5. $2x^2 - 3y^2 - xy + 4yz - xz$                         |                                |
| 6. (i) 5   | (ii) 727                       |
| 7. (i) $8x^2 - 34x + 30$                                 | (ii) $a^4 + 2a^2 - 15$         |
| 8. (a) 7   | (b) 47                         |

- |                       |                                 |
|-----------------------|---------------------------------|
| 9. (i) 77400          | (ii) 8200                       |
| 10. (i) 103           | (ii) 93                         |
| 11. (i) $x^4 - 1$     | (ii) $x^4 - 81$                 |
| 12. (i) 2.48          | (ii) 2400                       |
| 13. 49                | 14. 9                           |
| 15. 9.59              |                                 |
| 16. (a) $2a^2 + 2b^2$ | (b) $4ab$                       |
| 17. 7                 | 18. $x^{12} - \frac{1}{x^{12}}$ |
| 19. 6                 | 20. $\frac{15}{4}$              |

### Internal Assessment

Q1. Answer True (T) or False (F)

(a)  $x^2 + \frac{1}{x} = 5$  is a polynomial. (....)

(b)  $(x - 4)^2 = x^2 - 8x + 16$  (....)

(c) Coefficient of  $x^2$  in  $\frac{1}{2}x^2 + x$  is  $\frac{1}{2}$ . (....)

(d) Degree of the polynomial  $x^3 + x^2y - 5$  is 2. (...)

(e)  $(a + b)^2 - (a - b)^2 = 4ab$ . (...)

Q2. If  $x - \frac{1}{x} = 2$ , then the value of  $x^2 + \frac{1}{x^2}$  is

(i) 4 (ii) 2

(iii)  $\frac{1}{2}$  (iv)  $\frac{1}{4}$

Q3. If  $13x = (58)^2 - (45)^2$ , then  $x$  equals to

(i) 101 (ii) 102

(iii) 103 (iv) 104

Q4. The value of  $(x - 2)(x + 2)(x^2 + 4)$  is

(i)  $x^2 - 16$  (ii)  $x^2 + 4$

(iii)  $x^4 - 16$  (iv)  $x^4 + 16$

Q5. The value of  $a(b - c) + b(c - a) + c(a - b)$  is

(i)  $a^2 - b^2$  (ii) 0

(iii) 1 (iv)  $a^4 - b^4$

Q6. The value of  $(x - 4)(x + 5)$  is

(i)  $x^2 + x - 20$  (ii)  $x^2 - x + 20$

(iii)  $x^2 + 9x - 20$  (iv)  $x^2 - 9x + 20$

Q7. For  $x = -1$ , the value of  $x^3 - 2x^2 - 1$  is

(i) -4 (ii) 0

(iii) 2 (iv) 6

Q8. Length and breadth of a rectangle are  $(x + 3)$  and  $(x + 2)$  respectively, then its area is

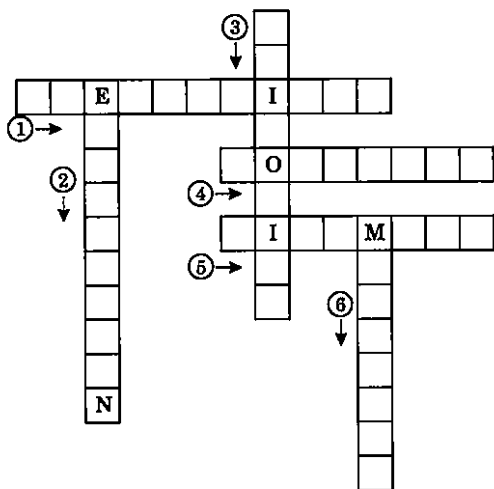
(i)  $x^2 - 5x + 5$  (ii)  $x^2 + x - 5$

(iii)  $x^2 + 5x + 6$  (iv)  $x^2 - x - 5$

Q9. The value of  $\frac{6.4 \times 6.4 - 3.6 \times 3.6}{2.8}$  is

- (i) 10 (ii) 12  
(iii) 16.4 (iv) 0

Q10. Complete the following crossword puzzle.



### Hints

- 5 is the \_\_\_\_\_ of  $5x^2y$
- $x^2 + x - 3$  is the algebraic \_\_\_\_\_ of degree 2.
- $x + xy + yz$  is \_\_\_\_\_ expressions.
- The \_\_\_\_\_ term in  $x^2 + 1$  is 1.
- $a + 2b$  is the \_\_\_\_\_ expression.
- $-5x$  is the \_\_\_\_\_ expression.

### ANSWERS

- (a) False (b) True (c) True  
(d) False (e) True
  - (i) 3. (iii)
  - (iii) 5. (ii)
  - (i) 7. (i)
  - (ii) 9. (i)
10. 1. COEFFICIENT 2. EXPRESSION  
3. TRINOMIAL 4. CONSTANT  
5. BINOMIAL 6. MONOMIAL